

# Corrigenda for “Distributional differential algebraic equations”

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- p. 46 In ninth line from the bottom it should read  $\delta_t$  instead of  $\delta_t^{(n)}$
- p. 61 The  $\square_{\text{qed}}$ -symbol should be at the end of the equivalence
- Sec. 4.2.1 see also Vinicius A. Armentano ”The pencil (sE-A) and controllability-observability for generalized linear systems: A geometric approach”, Siam J. Control and Optimization 24(4), p. 616–638
- p. 83 In the fifth line from below it should be  $\dot{x}_{[t_0, \infty)} = (Ax + f)_{[t_0, \infty)}$  instead of  $\dot{x}_{[t_0, \infty)} = (Ax)_{[t_0, \infty)}$ .
- p. 106 The name of Lemma 4.2.3 should read “Invertibility of  $[V, W]$  and  $[EV, AW]$ ”, furthermore the **proof is not complete**. The complete proof reads as:

Invertibility and existence of  $T$  follows from Lemma 4.2.2(ii). To show invertibility of  $[EV, AW]$  it is first shown that  $EV$  and  $AW$  each have full column rank. Therefore, consider  $x \in \mathbb{R}^{n_1}$  and  $y \in \mathbb{R}^{n-n_1}$  with  $EVx = 0$  and  $AWy = 0$ . Invoking Lemma 4.2.2(ii) yields  $Vx \in \mathcal{V}^* \cap \ker E = \{0\}$  and  $Wy \in \mathcal{W}^* \cap \ker A = \{0\}$ . Since  $V$  and  $W$  have full column rank it follows that  $x = 0$  and  $y = 0$ , hence  $EV$  and  $AW$  have full rank. It remains to show that  $EV^* \cap AW^* = \{0\}$ . Therefore, consider  $x \in EV^* \cap AW^*$ . Then there exists  $v \in \mathcal{V}^*$  and  $w \in \mathcal{W}^*$  with  $Ev = x = Aw$ , in particular  $v \in E^{-1}(AW^*) = \mathcal{W}^*$ . Hence  $v \in \mathcal{V}^* \cap \mathcal{W}^* = \{0\}$  and  $x = 0$  follows.

- p. 112 several  $J$ s are missing, it should read:

hence, invoking Corollary 2.3.5,

$$(v(t+) - v(t-))\delta_t + \sum_{k=0}^K a_k \delta_t^{(k+1)} = \sum_{k=0}^K J a_k \delta_t^{(k)},$$

or

$$0 = \sum_{k=0}^{K+1} b_k \delta_t^{(k)},$$

where  $b_{N+1} = a_N$ ,  $b_k = a_{k-1} - J a_k$ ,  $k = N, \dots, 1$ , and  $b_0 = v(t+) - v(t-) - J a_0$ .

p. 114

in the third and fourth equation it should read  $n_2$  instead of  $n_1$ , and, in line seven, extend 'since  $N$  is nilpotent' to "since  $N \in \mathbb{R}^{n_2 \times n_2}$ ,  $n_2 \in \mathbb{N}$ , is nilpotent", finally, in the fifth equation, replace  $S$  by  $S^{-1}$ , i.e. it should read

Repeating this process yields, since  $N \in \mathbb{R}^{n_2 \times n_2}$ ,  $n_2 \in \mathbb{N}$ , is nilpotent,

$$0 = N^{n_2}(w[t_i])^{(n_2)} = w[t_i] - \sum_{k=0}^{n_2-1} N^{k+1}(w(t_i+) - w(t_i-))\delta_{t_i}^{(k)}$$

or

$$w[t_i] = \sum_{k=0}^{n_2-1} N^{k+1}(w(t_i+) - w(t_i-))\delta_{t_i}^{(k)}.$$

Assumption (A1) and Theorem 4.2.8 yield

$$\begin{aligned} 0 &\stackrel{(A1)}{=} E_p(I - \Pi_p)x(t_i-) \stackrel{\text{Thm. 4.2.8}}{=} E_p((x(t_i-) - x(t_i+))) \\ &= S^{-1} \begin{bmatrix} I & 0 \\ 0 & N \end{bmatrix} \begin{pmatrix} v(t_i-) - v(t_i+) \\ w(t_i-) - w(t_i+) \end{pmatrix} \end{aligned}$$

p. 144

in the second last line it should read " $\delta_{t_0}^{(i)}$ " instead of ' $\delta_{t_0}^i$ ' ,

p. 145

in the first line it should read " $\delta_{t_0}^{(i+1)}$ " instead of ' $\delta_{t_0}^{i+1}$ ' ,

p. 149

in Prop. 5.2.4 the first 'impulse-observable' should read "jump-observable", furthermore in (5.2.3) it should read " $x[t_0] = 0$ " instead of ' $w[t_0] = 0$ '

p. 164

just before Theorem 5.3.12 it should read "characterizations" instead of "characterization"

p. 167

in the sixth line of Remark 5.3.14 it should read  $x_2$  instead of  $\omega$  and in the last line of this page it should read  $x_4$  instead of  $\omega$